1 Perspectives on the mechanistic underpinnings of choice biases

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12 Abstract

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14 Early foundational work in the decision sciences carefully balanced empirical observations 15 and theoretical explanations. Dating back to Daniel Bernoulli, a handful of behavioral 16 regularities observed in theoretical lotteries ignited the refinement of normative theories and 17 the development of new descriptive frameworks of valuation and choice. However, more 18 recent tendencies in behavioral economics and psychology place empirical observations on a 19 pedestal: modern behavioral science has identified more behavioral biases than it has 20 explained. Coupled with replication and reliability crises in experimental psychology, this has 21 resulted in an explanatory gap in the field, in-between the descriptive and predictive levels. 22 Here, we aim to close this explanatory gap by asking how choice biases can emerge from 23 certain decision computations. We demonstrate that biased and irrational choice behavior may 24 arise from multiple, equally viable mechanisms, such as relative value coding and selective 25 information sampling. We posit that this "multiple realizability" problem highlights a broader 26 issue: inferring mechanisms of complex behavior solely from behavioral measures is an 27 underdetermined exercise. We propose that using time-resolved neural recordings to track 28 how attention serially parses complex information during multiattribute, multialternative 29 decisions can resolve this "multiple realizability" issue and arbitrate between competing 30 mechanistic explanations of choice biases.

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32 **1. Introduction**

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34 A large body of research within the cognitive and decision sciences has established that 35 human decisions are often influenced by factors that should rationally be ignored (De Martino 36 et al., 2006; Kahneman & Tversky, 1984; Summerfield & Tsetsos, 2015; Tversky & Kahneman, 37 1981). For example, we tend to stick with an energy plan because it is set as the default option 38 (Baron & Ritov, 1994), we prefer volatile stocks when buying but dismiss them when selling 39 (Shafir et al., 1993; Tsetsos, Chater, et al., 2012), or we choose salmon fillet over ribeye steak 40 simply because we noticed that fish fingers are also available (Huber et al., 1982). These 41 examples illustrate that choices are not solely determined by the properties of the available 42 alternatives and the goals of the decision-maker but also by an array of normatively irrelevant 43 factors including: the way the alternatives are presented, the framing of the choice, or the 44 presence of dominated (inferior) alternatives in the choice-set (Usher et al., 2019).

The observed sensitivity of human decisions to normatively irrelevant factors (reflected in *choice biases*) has had profound impact on the behavioral sciences, resulting in the distinction between normative (how *should* we decide) and descriptive (how *do* we decide) 48 theories of choice. One of the main goals of descriptive theories of choice is to specify how 49 choice biases come about in the deciding brain. Achieving this goal can subsequently inform 50 deeper multidisciplinary considerations, e.g., on why bias propensity varies among individuals 51 (Aczel et al., 2015; Spektor et al., 2021) or across the lifespan (Parrish et al., 2024; Tentori et 52 al., 2001); or on why biases have persisted despite evolutionary pressure for rewardmaximizing choices (Moran & Tsetsos, 2018; Tsetsos et al., 2016; Webb et al., 2021). 53 54 Furthermore, choice biases have taken center stage in applied behavioral science, 55 representing predictable blind spots that can be harnessed in interventions to induce 56 behavioral change (Thaler & Sunstein, 2009). Precisely understanding the mechanisms that 57 mediate choice biases can aid the development of targeted approaches that could bolster the 58 limited effectiveness of extant "nudging" interventions (Maier et al., 2022).

59 Despite the theoretical and applied importance of understanding the computational 60 and neural mechanisms that lead to choice biases, existing theories of choice have not 61 provided definitive insights. This is reflected in the multitude and disparity of frameworks 62 proposed to explain choice biases, ranging from verbally formulated heuristics (Gigerenzer & 63 Gaissmaier, 2011; Kahneman & Tversky, 1984; Shafir et al., 1993) and algebraic modifications 64 of normative theories (Tversky & Kahneman, 1992; Tversky & Simonson, 1993) to Bayesian (Bhui & Xiang, 2021; Srivastava & Schrater, 2012) and dynamical models (Busemeyer et al., 65 2019). To date, these disparate explanations of choice biases, often casted at different levels 66 67 of analyses (McClelland, 2009), have not been comprehensively related to underlying decision 68 mechanisms. In this chapter, we aim to close this gap by describing how explanations of 69 hallmark choice biases can be situated along the processing stages that occur during decisionmaking. 70

71 We begin by clarifying the notion of choice bias and proceed to show that hallmark 72 choice biases could fall out from computations occurring at almost any stage-including 73 relative and non-linear value coding (Louie & De Martino, 2014), selective information 74 sampling (Usher et al., 2019), and non-linear accumulation dynamics (Cavanagh et al., 2020). 75 Given this "multiple realizability" issue, we then address how distorting mechanisms along the 76 processing pathway can be better identified. We highlight that during complex decisions, 77 information is sampled partially and serially before reaching the decision formation level; and 78 propose that tracing this information flow with non-invasive high-temporal-resolution neural 79 recordings as decisions unfold can considerably constrain mechanistic inferences. We 80 conclude that a central goal in the cognitive and neural sciences should be to understand the 81 principles that orchestrate information sampling during decision-making.

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83 **2. Choice biases: innocuous and irrational**

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85 From a normative standpoint, an optimal agent should always (or more likely, in the presence of behavioral stochasticity (Loomes & Sugden, 1995)) choose the most desirable course of 86 87 action in any given situation (Summerfield & Tsetsos, 2015). Thus, a prerequisite of optimal 88 behavior is the ability to value choice alternatives by transforming their objective properties 89 into "desirability" (or utility) scores based on a set of criteria that represent the goals and needs 90 of the agent at any given moment (Juechems & Summerfield, 2019). A longstanding question 91 in the decision sciences is whether human choices comply with this notion of optimality. This 92 has been hard to assess since, in real-life decisions, decision-relevant criteria are inherently 93 subjective and opaque. To circumvent this issue, decision theorists have resorted to two 94 distinct approaches: i) studying choice behavior in simplified scenarios where decision95 relevant criteria can be objectively defined; ii) specifying a set of rules (or axioms) that utility-

- 96 maximizing agents must abide by. In the following, we define choice biases in relation to these
- 97 two approaches.
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99 2.1 Innocuous biases

100 To study human valuation and choice in a tractable way, researchers often rely on laboratory 101 tasks with externally imposed objectives (Summerfield & Tsetsos, 2012). This approach has 102 roots in the foundational years of probability theory, where theoretical lotteries were used to 103 benchmark human behavior against statistical optimality (Stearns, 2000). In these cases, it 104 can be assumed that the desirability of each lottery option is equivalent to the expected value 105 of the corresponding payout distribution. Thus, statistically optimal agents should always 106 choose the lottery with the largest expected value. However, even in these tractable situations, 107 human choices depart from the statistical ideal. Consider a choice between two prospects A 108 and B. Prospect A offers £40 for sure while prospect B offers £100 with 50% probability or £0 109 otherwise. Although prospect B has a higher expected value ($EV_A = \pounds 40$ vs. $EV_B = \pounds 50$), most people in this scenario will choose prospect A (Kahneman & Tversky, 1979) (Fig. 1A). This 110 111 example illustrates that human valuation is sensitive to the variances of the payout 112 distributions, which is not relevant for maximizing expected rewards. More broadly, human 113 economic choices disclose several idiosyncrasies, such as risk (Mata et al., 2018) and 114 skewness preferences (Olschewski et al., 2024) or aversion to losses (Novemsky & 115 Kahneman, 2005).

116 Idiosyncratic biases are not specific to theoretical lotteries but can be encountered in 117 any choice task entailing a transparently defined payoff structure. In perceptual choice tasks, 118 participants observe sensory evidence and are asked to make choices based on a criterion 119 defined by the experimenter (e.g., choose the rectangle with the larger area). In these tasks, 120 humans and other animals exhibit several suboptimal tendencies that prevent them from 121 attaining optimal performance. For instance, across consecutive decisions, they exhibit choice 122 history biases (e.g., repeating or avoiding a previous choice) (Braun et al., 2018; Urai et al., 123 2019); or, within a decision, they assign larger weight to information presented early in the trial 124 (Tsetsos, Gao, et al., 2012). Similarly, in value-learning (bandit) tasks the objective of 125 maximizing monetary reward is undermined by a list of suboptimal tendencies such as ignoring 126 infrequent rewards or penalties (Hertwig et al., 2004), or overestimating the importance of 127 extreme outcomes (Ludvig et al., 2014).

128 The presence of this type of choice biases in tasks with clearly defined objectives 129 underlines that "desirability" is an inescapably subjective notion. That is, even when the task 130 dictates maximizing economic value, people will not limit themselves to just that. Instead, in 131 addition to accruing economic value, people seem to be gaining extra utility by avoiding risky 132 prospects and losses, by repeating their previous choices, or by avoiding committing errors in 133 perceptual choices at the expense of dwelling for too long on a given decision (Bogacz et al., 134 2010). Although these tendencies lead to biased choices and curtail reward accrual, they may satisfy other latent, non-economic metrics. Thus, biased choice behavior can be "rationalized" 135 136 as maximizing a stable, albeit idiosyncratic, utility function. Because the kind of choice biases 137 we reviewed here do not rule out utility-maximizing behavior under a more liberal definition of 138 utility, we deem them *innocuous*¹.

¹ The point that choice biases reflect idiosyncratic preferences for non-normative aspects is rather theoretical, aiming to emphasise that the presence of certain biases does not falsify an expanded notion



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141 Figure 1. Illustrative examples of innocuous and irrational choice biases. (A) A stable concave 142 (diminishing returns) utility function predicts a risk-aversion bias in a choice between two hypothetical 143 gambles with explicitly described rewards and probabilities. (B) Contextual preference reversal in multiattribute choice. Alternatives vary across two attributes. For illustration purposes, we assume that 144 145 any two alternatives positioned on the negative diagonal are equally preferred in the respective binary choices. The attraction effect is a choice bias for a target alternative A over a competitor B occurring in 146 147 ternary choices after an inferior decoy (D_A) is introduced near the target. The similarity effect is a choice 148 bias for the target A after a non-dominated decoy (S_A) is introduced near the competitor B. The 149 compromise effect is a choice bias for the all-average alternative C over A or B, occurring in ternary 150 trials featuring another extreme alternative B. 151

152 2.2 Irrational biases

153 As described above, prominent choice biases can be absorbed into a putative utility function 154 that the agent's choices could be maximizing. Is the premise of utility-maximization even 155 falsifiable? In their influential work on rational choice theory, von Neumann and Morgenstern 156 demonstrated that the premise of utility-maximization is falsifiable: it can hold only if 157 preferences (as revealed by overt choices) satisfy certain rationality axioms (Savage, 1972; 158 von Neumann & Morgenstern, 2007). A stable utility function can be defined only when 159 preferences satisfy these axioms. Accordingly, if preferences violate any of these axioms, then the utility-maximizing narrative falls apart. In the below we adopt a bird's-eye-view and 160 161 describe the core intuition underlying the axioms of rational choice theory. More detailed and

of optimal (utility-maximizing) behavior. Practically, certain choice biases likely stem from processing bottlenecks in biological brains rather than from explicit preferences for non-normative aspects.

162 formal expositions of these axioms can be found elsewhere (Regenwetter & Davis-Stober,163 2012; Rieskamp et al., 2006).

164 Rational choice theory axioms are not concerned with the specific preferences of 165 agents but with the internal consistency (or rationality) of those preferences (Allingham, 2002). 166 Thus, they do not prescribe how choice alternatives should be mapped onto utilities; instead, 167 they just ensure that this mapping does not change due to irrelevant factors. One such 168 irrelevant factor is the choice framing (Kahneman & Tversky, 1984). Do preferences change 169 when a choice is framed as "select the best" versus when it is framed as "reject the worst"? 170 According to rational choice theory, in both frames, one should consider their needs and wants 171 and assign utility scores to alternatives. In the "selection" frame the alternative with the highest 172 score should be chosen, and in the logically equivalent "rejection" frame, the alternative with 173 the lowest utility score should be eliminated. Thus, when two alternatives are available, 174 selecting A coheres with rejecting B, and vice versa. However, it has been shown that when 175 alternative A is mediocre (e.g., a not-so-expensive and dull holiday destination) and B is more 176 extreme (e.g., an expensive but exciting destination) people tend to both select and reject the 177 extreme alternative (Shafir, 1993; Tsetsos, Chater, et al., 2012). This behavioral pattern 178 discloses inconsistent preferences and cannot be reconciled under the maximization of a 179 stable utility function that rational choice theory anticipates.

180 A second factor that provokes inconsistent choice patterns is the composition of the 181 choice-set. Following the rational choice schema, the utility assigned to an alternative should 182 solely be a function of its inherent properties and the goals and needs of the decision-maker. The utility of an alternative should thus be independent of the properties of other alternatives 183 184 that are available for choice (i.e., the independence-from-irrelevant-alternatives axiom). A 185 logical consequence of this schema is that if A is preferred over B when only these two 186 alternatives are offered, then A should still be preferred over B when a third alternative C is 187 available for choice. However, it has been shown time and again-even in non-primate 188 species including amoebae and bees (Latty & Beekman, 2011; Tan et al., 2015)-that 189 preferences change as a function of the choice-set composition (Evangelidis et al., 2024). To 190 illustrate, a preference for an all-inclusive holiday to Berlin (A) over an all-inclusive holiday to 191 Rome (B) can reverse when a holiday to Rome where you must pay for breakfast (C) is 192 introduced in the choice-set. In this example, the presence of the inferior alternative (C) boosts 193 the desirability of its more similar alternative (B). This so-called attraction effect (Huber et al., 194 1982) (Fig. 1B) and similar phenomena where preferences change as alternatives are added 195 or removed from the choice-set, are collectively referred to as contextual preference reversals 196 (Tsetsos et al., 2010). Unlike innocuous biases, the framing and choice-set preference 197 reversals outlined here are puzzling as they cannot be "rationalized" under a utility-maximizing 198 narrative. Therefore, we deem these choice biases irrational. An open question, which we will 199 explore in the next sections, is whether innocuous and irrational biases have distinct or 200 common mechanistic underpinnings.

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202 **2.3 Limitations in existing accounts of choice biases**

Within the judgment and decision-making literature, mainstay accounts of biased behavior consist of ad-hoc formulations that effectively re-describe human behavior without providing deeper explanations. For example, the "take-the-best" heuristic posits that decisions are settled exclusively based on the most important cue or attribute (Gigerenzer & Goldstein, 1996). Accordingly, it is assumed that people actively *use* this heuristic rule when making multiattribute decisions. In this case, the explanation (take-the-best heuristic) and the 209 explanandum (choice bias in favor of the alternative that is better in the most important 210 attribute) are almost indiscernible. This issue is not exclusive to the heuristic and biases 211 framework: in experience-based decisions (Hertwig & Erev, 2009) certain behavioral 212 regularities (e.g., recency or ignoring rare events) are ascribed to homologue processing 213 biases (i.e., underweighting early and rare events); or in algebraic models like in Prospect 214 Theory (Kahneman & Tversky, 1979), the shape of psychoeconomic functions and the position 215 of the reference point fit the patterns of human behavior but have no a priori motivation. Thus, 216 extant influential accounts of choice biases stay too close to the observed behavioral effects, 217 offering little explanatory depth.

Here, we do not claim that ad-hoc accounts should be dispensed with as they provide a useful and abstract way to summarize how human behavior deviates from the normative expectations. It is even conceivable that certain ad-hoc formulations, like explicit lossaversion, reflect hardwired asymmetries in the way the brain processes information (Tom et al., 2007). Instead, we posit that this level of theorizing cannot readily provide an encompassing answer to the question: how do choice biases occur in the deciding brain? In the next section we sketch an alternative and deeper level of theorizing choice biases.

226 **3. Mechanistic explanations of choice biases**

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228 Here we explore the idea that choice biases *emerge* from dynamic decision computations 229 rather than stemming from a rigid set of ad-hoc rules. This approach can have multiple 230 advantages. First, it can afford precise quantitative predictions, which can be valuable in 231 predicting novel biases or in anticipating how people would respond in different contexts. 232 Second, it can offer a natural interface between behavioral and neural levels (Gold & Shadlen, 233 2007), enabling the understanding of altered decision-making during ageing or in 234 neuropsychiatric disorders. Third, with certain decision computations serving adaptive 235 functions in biological brains (Summerfield & Tsetsos, 2020), linking choice biases to these 236 computations can help reconcile the normative-descriptive gap. Finally, a mechanistic 237 framework can, in principle, offer unifying and parsimonious explanations. Multiple choice 238 biases can arise from variations in a single or a minimal set of mechanisms, thereby reducing 239 the dimensionality of the tangled ontology of behavioral biases (Hallsworth, 2023).

240 However, to a large extent, mechanistic inferences are under-constrained by empirical 241 data (Pirrone & Tsetsos, 2023), especially in relatively complex behavioral domains (e.g., 242 multiattribute choices where choice biases abound). As a result, mechanistic models can 243 become overparametrized and arbitrary (Anderson, 2013), often ending up as ad-hoc as 244 heuristic formulations. Indeed, several influential multiattribute models can be criticized for 245 being overly flexible, combining algebraic ad-hoc and dynamic (and biologically grounded) 246 mechanisms to explain preference reversals (Roe et al., 2001; Trueblood et al., 2014; Usher 247 & McClelland, 2004). Even though we acknowledge the merit and influence of these more 248 complex models (for a comprehensive review see Busemeyer et al., 2019), we here consider 249 choice biases within the minimal evidence-accumulation framework developed for simple 250 perceptual decisions. We then expand this framework with a small set of additional 251 mechanisms intended to help agents navigate the rich information involved in multiattribute, 252 multialternative decisions.

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256 **3.1 Information processing during decision-making**

In a very generic description of the decision process, choices arise from first assigning utilities 257 258 to available alternatives (valuation) and then selecting the alternative that has the highest utility (comparison) (Platt & Plassmann, 2014; Vlaev et al., 2011). In most choice theories in 259 260 psychology and economics, valuation and comparison are formulated in a stylized fashion 261 using algebraic operations and functions (such as weighted summation, Keeney & Raiffa, 262 1993; or the softmax function). In contrast to these static and stylized formulations, 263 representations and computations in biological brains are shaped by noisy and dynamical processes (Miller et al., 2024). What are the dynamical processes underpinning decision-264 265 making?

266 Akin to biologists using the Drosophila as their model organism for studying more 267 complex organisms, psychologists and neuroscientists have used simple sensorimotor 268 decisions to approximate generalizable decision processes (Shadlen & Kiani, 2013). 269 Behavioral and neural data (Platt & Glimcher, 1999; Ratcliff & McKoon, 2008; Yang & Shadlen, 270 2007) indicate that during simple decisions—such as categorizing an ambiguous image as a 271 face or a house or determining the dominant direction of motion in a random dot kinematogram 272 (Heekeren et al., 2008)-noisy information is sampled and accumulated over time into a growing confidence signal, until a criterial degree of confidence (or *boundary*) is reached. 273 274 Following the law of large numbers, accumulation over time alleviates the detrimental 275 influence of noise and improves decision accuracy. The boundary on confidence controls how 276 long accumulation lasts for, effectively determining how the observer trades off the speed and 277 accuracy of the decision (Bogacz et al., 2010).

278 Within this *accumulation-to-bound* framework, valuation and comparison are dynamic 279 and temporally multiplexed processes. Valuation arises from *representing*², *sampling*³ and 280 accumulating noisy evidence (held in different accumulators) in favor of the available choice 281 alternatives (Fig. 2A). Choices are made once the activity of one of the accumulators exceeds 282 the decision boundary, thereby implementing the comparison operation (Lo & Wang, 2006). The specifics implementation of the comparison process can vary across models, particularly 283 284 in the form and degree of competition among the accumulators (Teodorescu & Usher, 2013). 285 Having outlined the fundamental mechanisms implicated in simple decisions, we next ask how 286 these mechanisms can lead to choice biases.

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² In any decision-task, external information needs to be mapped onto decision-relevant information. For example, if the task is to determine the rectangle that has the largest width, then information about the height or color of the rectangles is not relevant and needs to be discarded. Neural representations are subject to non-linear transduction, typically captured by a concave (e.g., logarithmic) transformation of the objective information (see Weber-Fechner law).

³ Decision tasks can entail either dynamic or static information. Dynamic information is naturally chunked into monetary samples, which are subject to serial accumulation. In static tasks, such as a face/house discrimination based on an ambiguous photograph, the assumption is that internal sampling turns takes noisy snapshots of the external information, which are then serially accumulated over time.



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290 Figure 2. Choice biases within a generalized mechanistic framework. (A) Schematic of the processing 291 hierarchy in decision-making: from stimulus representation to sampling, evidence accumulation, and 292 ultimately, choice. (B) The leaky competing accumulator (LCA) model architecture. "I" denotes lateral-293 inhibitory connections and "E" self-excitatory connections. With self-excitation being < 1, information is 294 subject to dissipation (leakage). The balance between leakage and lateral inhibition strength controls 295 the profile of temporal weighting (see main text). (C) Risk preferences within a bounded accumulation 296 framework. In the example scenario a high-variance (red) and a low-variance (blue) alternative compete 297 for choice. Following an initial pre-decisional period (left relative to the dashed vertical line), evidence 298 is accumulated in two accumulators that are weakly coupled with inhibition. Under the selection 299 (rejection) framing, once an accumulator breaches the upper (lower) boundary a selection choice is 300 made in its favor. The high-variance accumulator has large deflections and thus exceeds both 301 boundaries more often than the low-variance accumulator. This predicts risk-seeking under selection 302 and risk-aversion under rejection.

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305 3.2 Choice biases within the standard mechanistic framework

306 Can the standard mechanistic framework outlined above produce innocuous and irrational 307 choice biases? At first glance, this seems like a tall order for accumulation-to-bound models 308 because they essentially stem from the framework of optimal sequential hypothesis testing 309 (Bogacz et al., 2006; Wald, 2004; Wald & Wolfowitz, 1948). However, as described above, 310 accumulation-to-bound models can vary in their implementational details. Due to such 311 variations, some accumulation-to-bound models can deviate from statistically optimal 312 computations.

313 One characteristic example of suboptimal computations is the non-uniform temporal 314 weighting of evidence emerging from the accumulation dynamics in competing accumulator 315 models. In the leaky competing accumulator model (Usher & McClelland, 2001), the activity 316 of a given accumulator increases with the corresponding incoming evidence and decreases 317 due to self-dissipating activity (or leakage) and lateral inhibition coming from competing 318 accumulators (Fig. 2B). When the leakage and inhibition are balanced, the model mimics the 319 diffusion model showing equal sensitivity to early and late evidence (Bogacz et al., 2007). 320 When the inhibition is stronger than the leakage, the model operates in an impulsive regime, 321 exhibiting larger sensitivity to early evidence (primacy) through strong winner-take-all 322 dynamics. Conversely, when the inhibition is weaker than the leakage, the model becomes 323 forgetful or "leaky", being more sensitive to late evidence (recency) (Tsetsos, Gao, et al., 324 2012). Similar temporal weighting profiles fall out from variations in the excitation/inhibition ratio in a biophysical cortical circuit model of evidence accumulation (Lam et al., 2022). 325

326 Non-uniform temporal weighting can lead to innocuous choice biases when decision-327 relevant information is processed in a fixed order. Consider the choice between an affordable 328 but dull holiday destination (A) and an expensive and exciting destination (B). If the price 329 information is conveyed first, agents with a primacy weighting profile will consistently choose 330 A. Interestingly, non-uniform temporal weighting can lead to irrational choice biases if the 331 framing of the task or the choice-set composition alters the order in which information is 332 processed. For example, an agent with a primacy profile will disclose a preference reversal if 333 they first process positive information (B is exciting) in the "select the best" framing and 334 negative information (*B* is expensive) in the "reject the worst" framing. Thus, deviations from 335 statistically optimal computations can open the door to both innocuous and irrational choice 336 biases, depending on certain assumptions about the order in which information is considered. 337 Irrespective of assumptions about the order of information processing, how can the standard 338 mechanistic framework produce well-established choice biases?

339 We consider the innocuous preferences that humans have towards less or more 340 variable alternatives. Empirical findings suggest that people are risk-averse in description-341 based lotteries but risk (variance)-seeking when value information is experienced sequentially 342 (Tsetsos, Chater, et al., 2012). For presentation purposes, we describe both choice biases 343 using a hypothetical choice between two holiday destinations. A preference for the mediocre 344 holiday destination A over the more extreme one B (risk-aversion) can be explained by a 345 concave transduction function that maps objective values onto internal subjective counterparts (see also footnote 2 and Fig. 1A). This is the classical explanation of risk-aversion adopted in 346 347 expected-utility theory and prospect theory (Kahneman & Tversky, 1979). Beyond this rather 348 rigid representational distortion, in Figure 2C we show how the opposite risk-seeking bias 349 (Tsetsos, Chater, et al., 2012) naturally emerges within a minimal accumulation-to-bound 350 framework involving two independent (or weakly competing) accumulators racing towards a 351 boundary. Due to its more variable input, the accumulator corresponding to the more extreme 352 alternative B shows larger deflections. These deflections translate into an increased likelihood 353 of crossing the decision boundary. Similarly, under a rejection frame-and assuming that 354 elimination happens when an accumulator breaches a lower boundary-B will be more 355 frequently eliminated resulting in an irrational (framing) reversal of risk preferences (Shafir, 356 1993).

A preference for the more variable alternative (*B*) can also arise within a biophysical cortical model of evidence accumulation due to convex evidence transduction and non-linear accumulation dynamics (Cavanagh et al., 2020). Although it is not obvious how the biophysical model could produce a framing reversal of this bias, this model can produce a choice-set reversal. In choices among three alternatives that vary in their decision values, increasing the value of the worst alternative improves the relative discrimination accuracy between the two highest-value alternatives (Chau et al., 2014) (but see Cao and Tsetsos (2022) for an alternative interpretation of this effect). This *positive distractor* effect violates the independence-from-irrelevant-alternatives principle. The biophysical model captures the positive distractor effect because increasing the value of the worst alternative raises the level of the pooled inhibition. This, in turn, adjusts the accumulation dynamics to a regime closer to optimal, approximating the diffusion model that achieves the highest discrimination accuracy (Bogacz et al., 2007).

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371 3.3 Choice biases within an extended mechanistic framework

372 We showed that some innocuous and irrational choice biases can emerge within the standard 373 accumulation-to-bound framework. However, this framework cannot readily explain 374 multiattribute choice-set reversals (Fig. 1B). Notably, the standard mechanistic framework was 375 built around simple choice tasks, where the amount of decision-relevant information typically 376 falls below the processing capacity of the cognitive system (Donner et al., 2009; Gold & 377 Shadlen, 2007). However, choice biases, especially irrational ones, occur in more complex 378 decision domains involving multiple (more than two) alternatives that often vary in more than 379 one attribute (Busemeyer et al., 2019). In these cases, parsing information in parallel becomes impossible and the cognitive system needs to find ways to efficiently navigate the increased 380 381 complexity given its processing bottlenecks. Below, we discuss two classes of mechanisms 382 that can help the brain efficiently process large amounts of information. As a byproduct, these 383 mechanisms enable dynamic and context-dependent valuation, and choice biases ensue.

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385 Relative coding

386 The first class of mechanisms, collectively referred to as relative coding (Summerfield & 387 Tsetsos, 2020), entails dynamic and non-linear distortions impacting the representation of 388 decision-relevant information. More specifically, in contrast to static and context-independent transduction non-linearities (see footnote 2), relative coding schemes adjust representations 389 as a function of the temporal (i.e., the recent history of stimulation) or the immediate (i.e., the 390 391 choice-set) context. The exact form of these adjustments is motivated by the theory of efficient 392 neural coding widely evidenced in sensory systems (Simoncelli, 2003). This theory states that 393 neurons minimize redundancy by increasing their representational resolution for the most 394 frequently occurring stimuli (Barlow, 1961). Below we provide an overview of prominent relative coding schemes with regards to choice biases. 395

396 In the divisive normalization model, the "raw" utility of each alternative is divided by the 397 sum of the raw utilities of all alternatives in the choice set (Louie et al., 2013). Therefore, the 398 model predicts that increasing the utility of the worst alternative reduces the discrimination 399 accuracy between the two high-utility alternatives, a negative distractor effect at odds with the 400 independence-from-irrelevant-alternatives axiom (but see Gluth et al. (2020) for a failure to 401 replicate this effect). In the range normalization model (Rustichini et al., 2017), raw utilities are 402 divided by the range of raw utilities (max - min) encountered in the choice-set, that way 403 producing a positive distractor effect (Fig. 3). The range normalization principle together with 404 auxiliary assumptions can also explain contextual preference reversals in multiattribute 405 choice, including the attraction, the similarity, and the compromise effects (Soltani et al., 2012) 406 (Fig. 1B). These multiattribute effects can also be captured by a recurrent version of the 407 divisive normalization model, where the attribute value of an alternative is divided by itself plus 408 the mean choice-set values on that attribute (Dumbalska et al., 2020). Practically, relative 409 coding schemes implement context-dependent utility functions thereby generating irrational choice biases. One downside of relative coding schemes is that they afford compressive
representations. Thus, these models cannot readily capture the risk-seeking bias obtained in
decisions from experience (Tsetsos, Chater, et al., 2012).

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417 Figure 3. Distractor effects under relative coding schemes. (A) In a ternary choice task, observers 418 choose one alternative among three candidates (A, B, and a distractor D) on each trial. The distractor's 419 value is always lower than the values of targets A and B, so it should not influence the choice between 420 A and B, as predicted by the baseline model in panel B. In a thought experiment, observers perform 421 this task in two additional contexts where the option values are multiplicatively scaled up by 3 or 5. This 422 manipulation creates an ideal situation for testing prominent normalization theories. The distractor effect 423 is defined as the change in sensitivity (slope measure of a Gaussian cumulative-density-function fit to 424 choice probabilities) to the value difference between A and B (fixed), modulated by changes in the 425 distractor value. (B) Divisive normalization assumes the option value is transformed into the mean firing 426 rate $\mu_i = KV_i/(\sigma_h + \Sigma wV_i)$, where V_i is the raw value of the option under consideration, K > 0, $\sigma_h > 0$, and 427 w > 0 represent gain, semi-saturation, and weight, respectively (Louie et al., 2013). When w = 0, the 428 model reduces to the baseline version, meaning the value coding is independent of other options in the 429 choice-set. Range normalization assumes $\mu_i = KV_i/(\sigma_h + w(max(V_i) - min(V_i)))$, meaning the denominator 430 involves the range of the values rather than the summation. Both normalization models predict an 431 increase in the distractor effect as the multiplicative factor increases, but they predict the distractor 432 effect in opposite directions. These very specific predictions can be contrasted with the predictions of 433 other non-normalization models of distractor effects (e.g., decision-by-sampling). Code for reproducing 434 this figure can be found at: https://github.com/YinanCao/bookchapter 435

436 Selective sampling

437 The second class of mechanisms we review operate downstream the early distortions that 438 relative coding schemes induce. These mechanisms govern selective information sampling 439 by determining, at each moment, which aspects of the available information should be passed on for accumulation. Selective information sampling is a pragmatic solution to the challenge 440 441 posed by the rich information involved in multialternative and multiattribute decisions. Indeed, 442 it is commonly observed that during complex decisions, attention serially traverses across 443 attributes and alternatives (Fiedler & Glöckner, 2012; Russo & Dosher, 1983), driving the 444 online construction of preferences (Slovic, 1995). Recent work has incorporated attentional 445 fluctuations into the accumulation-to-bound framework by positing that the gain of processing

increases for attended items (Krajbich et al., 2010). However, the principles that orchestrate
these attentional fluctuations, and the reasons why sampling can end up being partial and
biased, remain unknown. Below we review proposals that infer principles of information
sampling through explaining contextual preference reversals.

450 Various models of multiattribute choice assume that only one attribute can be 451 processed at a time, with attention stochastically fluctuating across attributes over time (Roe 452 et al., 2001; Turner et al., 2018; Tversky, 1972). More recent models additionally assume that 453 within each attended attribute, only a subset of the available alternatives is considered at a 454 given instance (Wollschläger & Diederich, 2012). In the decision-by-sampling multiattribute 455 model (Noguchi & Stewart, 2018), two alternatives are compared within each sampled 456 attribute, with more similar alternatives forming comparison pairs more frequently. The binary outcome of the comparison updates the "counting" accumulator of the winner. Due to these 457 458 principles and some auxiliary assumptions, the model can explain the attraction, similarity, 459 and compromise effects (Fig. 1B). A recent adaptation of the decision-by-sampling framework 460 can also explain a positive distractor effect in single-attribute decisions (Tohidi-Moghaddam & 461 Tsetsos, 2024). Another sampling model, the selective integration model, assumes that within 462 a focused attribute, attentional selection prioritizes the processing (i.e., assigns a larger gain) 463 of high-valued alternatives at the expense of low-valued alternatives, a principle that leads to 464 the attraction and other contextual preference reversal effects (Tsetsos, 2012; Tsetsos, 465 Chater, et al., 2012) including violations of transitivity (Tsetsos et al., 2016). The selective 466 integration model also predicts risk-seeking that reverses under a rejection frame where observers prioritize the processing of lower values (Usher et al., 2019). Taken together, in the 467 468 models described above, selective sampling leads to innocuous and irrational choice biases 469 by prioritizing the processing of certain choice aspects at the expense of others.

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4. Identifying the mechanisms underpinning choice biases

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The previous section highlights that, even within a limited search space of mechanisms, there are multiple and equally viable⁴ explanations for choice biases situated at all stages of the processing pathway (Table 1). This is a stark reminder that the cognitive and neural mechanisms of more complex behaviors are grossly underdetermined by empirical data (Pirrone & Tsetsos, 2023). How can the mechanisms underlying the various choice biases be securely identified?

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⁴ Here, arbitrating competing mechanisms based on auxiliary criteria, like biological plausibility or normative justification, seems fruitless. For instance, given efficient codes in the brain, two competing schemes, divisive and range normalization, seem equally biologically plausible. Similarly, while relative coding schemes can maximize information transfer while keeping metabolic costs bounded, the selective integration can maximize a different metric, namely decision accuracy in the presence of late noise (Tsetsos, K., Moran, R., Moreland, J., Chater, N., Usher, M., & Summerfield, C. (2016). Economic irrationality is optimal during noisy decision making. *Proc Natl Acad Sci U S A*, *113*(11), 3102-3107. https://doi.org/10.1073/pnas.1519157113).

Table 1. Summary of the standalone predictions of various mechanisms in relation to innocuous and
 irrational choice biases. "R" stands for representation, "S" for sampling, and "A" for accumulation. "?" is
 inserted when certain effects have not been adequately explored in relation to certain choice biases.

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Mechanism		Choice biases					
Stable non- linear function (R)		Risk- seeking (under selection)	Risk- aversion (under selection)	Framing risk- reversal	Negative distractor	Positive distractor	Multiattribute preference reversals
	Convex	Yes	No	No	No	No	No
Relative value coding (R)	Concave	No	Yes	No	No	No	No
	Divisive normalization	No	Yes	?	Yes	?	No
	Range normalization	No	Yes	?	No	Yes	Yes
	Recurrent divisive normalization	No	Yes	?	?	?	Yes
Selective							
	Selective integration	Yes	No	Yes	?	?	Yes
	Decision-by- sampling	?	?	?	No	Yes	Yes
Non-linear accumulation (A)							
	Bounded accumulator	Yes	No	Yes	No	No	No
	Biophysical cortical circuit	Yes	No	?	No	Yes	No

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491 Identifying the mechanisms that underlie a cognitive process requires the ability to 492 experimentally manipulate or observe the process input while simultaneously observing the 493 output at the behavioral and neural levels. As we alluded to in previous sections, this approach 494 is exemplified in the study of sensorimotor decisions, where the use of well-controlled 495 psychophysical stimuli have uncovered the neural underpinnings of perceptual decision-496 making (Gold & Shadlen, 2007). However, in multiattribute choice problems-which entail 497 information across different attributes and require comparisons between multiple 498 alternatives-the input to the decision process is not under experimental control. Instead, due 499 to the rich information exceeding the parallel processing capacities of the cognitive system, 500 attention can voluntarily fluctuate over time in numerous different ways (i.e., examining one 501 alternative on all attributes at a given time, dividing attention between two alternatives, 502 focusing on all alternatives in one attribute etc.). Observing these fluctuations is necessary to 503 uncover the flow of the input that drives the decision-making process. In turn, knowing the 504 dynamical input of the decision process can radically constrain mechanistic inferences and 505 answer how choice biases come about. Simply put, understanding how the brain processes 506 information requires knowing what information it processes.

507 Mainstay approaches have attempted to empirically characterize information sampling 508 using eye-tracking techniques. However, interpreting eye movements and fixations is not 509 straightforward in the context of decision-making tasks. Eye movements can also correspond 510 to operations unrelated to the decision-making process (i.e., merely reading the information), 511 which cannot be dissociated from decision-related oculomotor activity (i.e., accumulating the fixated information). Instead, it is often asserted that only fixations in the middle part of the 512 513 deliberation are decision-related, while early fixations correspond to the "scanning" stage and 514 late fixations to the "validation" stage (Bettman & Kakkar, 1977). Importantly, even if decision-515 related fixations could be dissociated from unrelated operations, knowing where people fixate 516 does not say much about what they think. Does looking at the price of holiday destination A 517 guarantees that the price of holiday B is not covertly considered at the same time in a 518 comparative manner?





526 amplitude measured at each sensor during the localizer task ("Training data") is modelled with spatial 527 channels, each selectively tuned to a different angular position. Next, the encoding model is inverted to 528 estimate the channel responses from the pattern of M/EEG signals across the scalp in another task 529 ("Test data"), such as multi-alternative decision-making or a classic bandit task in reinforcement 530 learning. Finally, neural gains projected spatially across the stimulus space are reconstructed for each 531 single trial. (B) Decoding performance revealed by training IEM on neural data vs. concurrent eye-gaze 532 data in the spatial localizer task. Upper panel: Topography shown as PCA loadings that maximally 533 differentiate between the three spatial stimulus locations, indicating where the neural activation patterns 534 across the scalp best diversify across these locations. Cross-validation shows that the IEM trained on 535 neural signals exhibits excellent and highly reliable decoding performance, peaking around 140 to 170 ms after stimulus onset, and is consistent across individual locations. In stark contrast, because the 536 537 localizer task prohibits eye movement, IEM trained on eye positions contains no decodable information 538 about stimulus locations (lower panel). This demonstrates that the method reliably captures covert 539 neural processes and neural gain modulation in the visual-parietal regions.

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541 Thus, eye-tracking techniques are limited to overt attention, while the computational 542 role of the tracked measures is unclear. What has been missing is a way to track both the 543 locus of attention (overt and covert) and at the same time the state of the accumulators as 544 complex decisions take shape. Recent work from our lab (Siems et al., 2023) and others 545 (Mostert et al., 2018) has offered new possibilities for continuously tracking the locus of covert 546 spatial attention using non-invasive neural recording techniques that have high temporal 547 resolution (magneto/electro-encephalography (M/EEG)). This relies on a dedicated functional 548 localizer task and an encoding model that is inverted to estimate the locus of attentional 549 allocation on a single trial basis from the pattern of M/EEG signals across the scalp in another 550 task, such as multialternative decision-making or a classic bandit task in reinforcement 551 learning (Fig. 4A). The key technical advantage of this approach is the clear dissociation of 552 covert processes from oculomotor "contaminations", with the spatial location decoding of 553 attention being robust across multiple locations and unaffected by eye gaze shifts, no matter 554 how minuscule they are (Fig. 4B). Combining the tracking of covert attention with well-555 established M/EEG signals that track the state of decision accumulators (e.g., the beta-band 556 lateralization in parietal and pre-motor cortices) (Donner et al., 2009; O'connell et al., 2012) 557 can reveal regularities and biases in information sampling (Siems et al., 2023), decisively 558 constraining mechanistic inferences about the general decisions processes as well as those 559 that generate innocuous and irrational choice biases. 560

- 561 **5. Conclusions**
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563 Research in behavioral economics and psychology has identified several choice biases that 564 still lack conclusive mechanistic explanations. In this chapter, we explored how choice biases 565 can be mapped onto the neural and computational mechanisms underlying decision-making. 566 Using as our starting point the standard accumulation-to-bound framework developed for simple decisions, we described how choice biases can emerge from decision computations 567 568 throughout the processing pathway: from representing, to sampling, to accumulating decision-569 relevant information. While non-linear accumulation dynamics within the standard 570 accumulation-to-bound framework can explain some choice biases, a more complete 571 explanation of irrational preference reversals requires invoking relative coding at the 572 representation level or selective information sampling. Given that relative coding and selective 573 sampling are both descriptively adequate, biologically plausible, and normatively motivated, distinguishing between these two types of mechanisms seems impossible. This resonates with 574 575 the broader issue that identifying the mechanisms underlying complex decision-making is

576 underdetermined, given that the effective input to the decision process is opaque and 577 intractable with conventional process tracing techniques. We outlined how using non-invasive 578 time-resolved neural recordings can track attentional fluctuations during decision-making, that 579 way measuring the effective decision input feeding to downstream decision computations.

580 We argue that observing how information is being sampled during complex decisions 581 can unlock the mechanistic understanding of puzzling behavioral regularities. As we described 582 in this chapter, non-linear accumulation dynamics can lead to non-uniform temporal weighting 583 of information (Tsetsos, Gao, et al., 2012). Across these lines, more recent findings suggest 584 that evidence accumulation is not simply a feed-forward process, with the state of downstream 585 accumulators biasing the way incoming evidence is weighted (Talluri et al., 2018). Thus, with 586 information being unequally weighted over time, the order in which information is being parsed 587 can be the major determinant of choice. If choice-set or framing manipulations do not 588 systematically alter the order of information sampling, then relative coding computations would 589 appear necessary to explain irrational choice biases. However, if framing and choice-set 590 manipulations systematically alter the order of information processing, then puzzling choice 591 biases could simply result from a combination of non-linear accumulation dynamics and 592 specific patterns of information sampling (presumably consistent with extant sampling 593 proposals, such as selective integration and decision-by-sampling). In this latter case, better 594 understanding the principles and mechanisms that orchestrate information sampling during 595 decision-making would become a critical new goal in the cognitive and decision sciences.

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